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# Channel Models for Multi-Level Cell Flash Memories Based on Empirical Error Analysis

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#### I. INTRODUCTION

Channel modeling for NAND flash memories is a developing research area with applications to better signal processing and coding techniques for flash memories. In [1], [2], the empirical cell threshold voltage distributions of multi-level cell (MLC) flash memories are modeled using known probability distributions to derive parametric channel models. The evaluation of such models is typically based on how well they are able to estimate/fit the empirically observed raw bit error rate (RBER) of the flash memory.

Analytical estimation of error-correcting code (ECC) frame error rate (FER) performance based on the RBER of a flash memory is hard especially for ECCs such as LDPC and Polar codes. Estimating the ECC FER performance for a flash memory experimentally using Monte-Carlo simulation techniques is also practically impossible due to the extremely large amount of empirical data required to estimate very low frame error rates (e.g.,  $10^{-10}$ ). Hence it is important to develop parametric channel models for flash memories that can provide accurate ECC FER performance estimates.

In this abstract, based on a detailed empirical error analysis of 2Y-nm MLC flash memory chips we observe and characterize the overdispersion phenomenon in the number of bit errors per ECC frame. Due to this overdispersion phenomenon, we show that the RBER of a flash memory chip is not a sufficiently good predictor of the ECC FER performance and hence a well studied binary discrete memoryless channel model such as the binary asymmetric channel (BAC) model is unable to provide acccurate ECC FER performance estimation. Hence we propose a binary discrete channel model based on the beta-binomial probability distribution (2-BBM channel model) and show using simulation results for BCH and LDPC codes, that the 2-BBM channel model provides accurate ECC FER performance estimation in MLC flash memories.

#### **II. EXPERIMENT PROCEDURE**

For error characterization, we perform program/erase (P/E) cycling of the MLC flash memory chip under test which consists of repeated application of the erase and program operations on the blocks under test. We also perform read operations at intervals of every 100 P/E cycles to record the bit error information. We arbitrarily select 4 contiguous blocks for our experiments and pseudo-random data is used for programming. The blocks are P/E cycled up to 10,000 P/E cycles at room temperature in a continuous manner with no extra wait time between the erase/program/read operations.

#### **III. ERROR CHARACTERIZATION**

In this section, we study the empirical bit error characteristics during P/E cycling in MLC flash memories. We represent the four charge levels in MLC flash memory as 0, 1, 2, 3 in the increasing order of charge levels respectively. The corresponding 2-bit patterns written to the lower and upper pages are '11', '10', '00' and '01' respectively. The two main characteristics studied are the asymmetry of bit errors and the distribution of number of bit errors per frame.

TABLE I ERROR CHARACTERIZATION RESULTS

(A)						( <b>B</b> )					
Write Cell	Read Cell Values					Frame Length, N = 8192					
Values	11	10	00	01		P/E Cycles	Lower Page		Upper Page		
11	0.00	18.39	0.03	4.01			Mean	Variance	Mean	Variance	
10	0.07	0.00	62.22	1.84		6000	14.85	29.64	7.18	10.23	
00	0.00	0.06	0.00	13.39		8000	30.03	84.81	14.46	24.37	
01	0.00	0.00	0.00	0.00		10000	52.61	216.95	26.06	51.30	

Table I(A) shows the frequency of cell errors measured as a percentage of total number of cell errors observed across all P/E cycles. We observe that there is asymmetry in the number of  $0 \rightarrow 1$  and  $1 \rightarrow 0$  bit errors in the lower page and, in the upper page, the degree of asymmetry is much lower. The number of bit errors per frame parameter is the key factor in determining the ECC FER performance. From P/E cycling experiment data, we obtain the sample mean and variance statistics of the number of bit errors per frame in both lower and upper pages as shown in Table I(B). We observe that the variance in

the number of bit errors per frame is much larger than the mean i.e., the experiment data is overdispersed with respect to a binomial distribution B(n, p) typically used to model count data whose variance  $\approx$  mean when p is small.

#### IV. CHANNEL MODELS FOR MLC FLASH MEMORIES

Based on the error characterization, we study a per-page BAC model and propose a per-page binary discrete channel model based on the beta-binomial probability distribution (2-BBM channel model) for MLC flash memories. Using empirical results and analysis, we show that the 2-BBM channel model is suitable for ECC FER performance estimation.

#### A. Definitions and Notation

Let K represent the total number of bit errors in a frame of length N bits. Let  $K_m$  be the total number of bit errors in a frame of N bits which consists of exactly m zeros. We denote the number of  $0 \rightarrow 1$  and  $1 \rightarrow 0$  bit errors in a frame with m zeros by  $K_m^{(0)}$  and  $K_m^{(1)}$  respectively. We have

$$K_m = K_m^{(0)} + K_m^{(1)} \tag{1}$$

where  $K_m \in \{0, 1, \ldots, N\}$ ,  $K_m^{(0)} \in \{0, 1, \ldots, m\}$  and  $K_m^{(1)} \in \{0, 1, \ldots, N - m\}$ . K can also be represented as the sum of the total number of  $0 \to 1$  and  $1 \to 0$  errors as

$$K = K^{(0)} + K^{(1)}$$
 where, (2)

$$\Pr(K^{(u)} = k) = \sum_{m=k}^{N} \frac{\binom{N}{l}}{2^{N}} \, \Pr(K_m^{(u)} = k) \tag{3}$$

where  $u \in \{0, 1\}$  and l = m + (N - 2m)u.

#### B. The 2-Binary Asymmetric Channel (2-BAC) Model

For the BAC model,  $K_m^{(0)}$  and  $K_m^{(1)}$  are distributed as per the binomial probability distribution and are independent i.e.,

$$K_m^{(0)} \sim B(m,p); \quad K_m^{(1)} \sim B(N-m,q); \quad K_m^{(0)} \perp K_m^{(1)}$$

where p and q denote the probabilities of  $0 \rightarrow 1$  and  $1 \rightarrow 0$  bit errors respectively and B(m, p), B(N - m, q) denote binomial probability distributions.

Proposition 1: The mean of K (E[K]) and the variance of K (Var[K]) for a BAC model are given by

$$\mathbf{E}[K] = \frac{N}{2}(p+q) \tag{4}$$

$$\operatorname{Var}[K] = \frac{N}{2} \left( (p+q) - pq - \frac{1}{2} (p^2 + q^2) \right)$$
(5)

The parameters of the BAC model p and q are estimated as the average  $0 \rightarrow 1$  and  $1 \rightarrow 0$  bit error rates obtained empirically. From proposition 1, Var[K] < E[K] and for small values of p and q,  $Var[K] \approx E[K]$ . Thus the 2-BAC model of a MLC flash memory does not fit the empirical observations in Table. I(B) and hence is unsuitable for accurate ECC FER performance estimation. However, note that the 2-BAC model does provide an accurate estimate of the average RBER which is given by  $\frac{E[K]}{N}$ . This shows that the ability to accurately estimate/predict the average RBER is not the sole criterion for a good MLC flash memory channel model.

#### C. The 2-Beta-Binomial (2-BBM) Channel Model

From the empirical error characterization results, we observed that the mean and the variance statistics of the number of bit errors per frame indicate overdispersion with respect to a binomial distribution. The beta-binomial probability distribution was first proposed in [3] as the probability distribution of counts resulting from a binomial distribution if the probability of success varies according to the beta distribution between sets of trials. Using empirical data, it was also shown in [3] that the beta-binomial probability distribution is suitable for modeling overdispersed count data. For the beta-binomial (BBM) channel model corresponding to the lower/upper page, we model the variables  $K_m^{(0)}$  and  $K_m^{(1)}$  as being distributed according to the beta-binomial distribution i.e.,

$$p \sim f(a,b); \quad K_m^{(0)} | p \sim B(m,p); \qquad K_m^{(0)} \sim B_f(m,a,b) q \sim f(c,d); \quad K_m^{(1)} | q \sim B(N-m,q); \quad K_m^{(1)} \sim B_f(N-m,c,d)$$

where f(a, b), B(m, p) and  $B_f(m, a, b)$  denote the beta, binomial and the beta-binomial probability distributions respectively (similarly f(c, d), B(N - m, q) and  $B_f(N - m, c, d)$ ). X | Y denotes "X given Y". The parameters a, b, c, d of the BBM channel model are estimated from the sample moments of  $K^{(0)}$  and  $K^{(1)}$  using the method of moments [3]. From empirical data, we obtain the sample mean and second moment estimates of  $K^{(0)}$  and  $K^{(1)}$ . Let  $\mu_1$ ,  $\mu_2$  represent the first and second moment estimates of  $K^{(0)}$  (similarly  $\mu_3$ ,  $\mu_4$  for  $K^{(1)}$ ). The parameter estimates are given by

$$\hat{a} = \frac{\mu_1^2(N+1) - 2\mu_1\mu_2}{N(\mu_2 - \mu_1) - \mu_1^2(N-1)}; \quad \hat{b} = \hat{a}\left(\frac{N}{2\mu_1} - 1\right)$$
(6)

$$\hat{c} = \frac{\mu_3^2(N+1) - 2\mu_3\mu_4}{N(\mu_4 - \mu_3) - \mu_3^2(N-1)}; \quad \hat{d} = \hat{c} \left(\frac{N}{2\mu_3} - 1\right)$$
(7)

#### D. ECC FER Performance Estimation Results

Fig. 1 shows the FER performance of a BCH code and a regular quasi-cyclic LDPC (QC-LDPC) code with  $d_c = 64$  and  $d_v = 4$  where  $d_c$  and  $d_v$  refer to the check node and variable node degrees respectively in the parity check matrix. For both the ECCs considered, we observe that the 2-BAC model provides an optimistic estimate of the FER performance when compared to the empirically observed FER performance. This is mainly due to the inability of the 2-BAC model to capture the high variance in the number of bit errors per frame observed empirically. From these results it is clear that the proposed 2-BBM channel model is able to accurately describe the nature of the number of bit errors per frame in MLC flash memories and hence provides accurate estimates of the ECC FER performance.



Fig. 1. Comparison of FER performance of a (N = 8191, k = 7683, t = 39) BCH code and a (N = 8192, k = 7683) regular QC-LDPC code using empirical error data and error data from simulation using the 2-BAC and the 2-BBM channel models.

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- [2] T. Parnell, N. Papandreou et al., "Modelling of the threshold voltage distributions of sub-20 nm NAND flash memory," in Proc. IEEE Global Communications Conference (GLOBECOM), Dec 2014, pp. 2351–2356.
- [3] J. G. Skellam, "A probability distribution derived from the binomial distribution by regarding the probability of success as variable between the sets of trials," *Journal of the Royal Statistical Society. Series B (Methodological)*, vol. 10, no. 2, pp. 257–261, 1948.

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### **Letter from the Director**



This newsletter comes at a time with many new activities as well as new and returning faces to CMRR. We also welcome back a eight graduate students who participated in in summer internships with a range of companies including **Westem Digital**, **Bosch**, **HGST**, **Cymer**, **SanDisk**, **Seagate**, **CNEX Labs** and **Spawar**. Their summer research covered much of the current research at CMRR. This strong interaction of our students with our industrial partners is a clear part of the CMRR mission to train students for the information technologies industries. I hope we continue to keep this strong participation of our students with our corporate sponsors in the coming years. We have a number of visitors coming to CMRR including Osamu Torii from Toshiba and Eitan Yaakobi from Technion University. This year, we are hosting eight new visiting graduate students and scholars. Welcome to all of you.

NVMW 2017 March 12-14, 2017 UCSD, Price Center East Ballroom



## **Selected Papers**

#### **Professor Eric Fullerton**

Mohammed Salah El Hadri, Michel Hehn, Philipp Pirro, Charles-Henri Lambert, Grégory Malinowski, **Eric E Fullerton**, and Stéphane Mangin, "Domain Size Criterion for the Observation of All-Optical Helicity-Dependent Switching in Magnetic Thin Films" *Physical Review B, Vol.94-Iss.6, PP.064419*, August 15, 2016.

SA Montoya, S Couture, JJ Chess, JCT Lee, N Kent, D Henze, SK Sinha, M-Y Im, SD Kevan, P Fischer, BJ McMorran, V Lomakin, S Roy, and EE Fullerton, "Dipolar-Stabilized Skyrmion and Skyrmion Lattice in Fe/Gd Multilayers" *arXiv preprint arXiv: 1608.01368*, August 03, 2016.

Rajasekhar Medapalli, Dymtro Afanasiev, Dokyun Kim, Yassine Quessab, Sergio A Monotoya, Andrei Kirilyuk, Theo Rasing, Alexey V Kimel, and Eric E Fullerton, "Mechanism of All-Optical Control of Ferromagnetic Multilayers with Circularly Polarized Light" arXiv preprint arXiv: 1607.02505, July 07, 2016.

Vojtech Uhlir, Jon Ander Arregi, and Eric E Fullerton, "Colossal Magnetic Phase Transition Asymmetry in Mesoscale FeRh Stripes" arXiv preprint arXiv: 1605.06823, May 22, 2016.

#### **Professor Vitaliy Lomakin**

Jordan J. Chess, Sergio A. Montoya, Tyler R, Harvey, Colin Ophus, Simon Couture, Vitaliy Lomakin, Eric E. Fullerton, and Benjamin J. McMorran, "A Streamlined Approach to Mapping the Magnetic Induction of Skyrmionic Material" *arXiv preprint arXiv:* 1608.06000, August 24, 2016.

Jin-Kyun Byun, Iana Volvach, and Vitaliy Lomakin, "Fast Optimal Design Micromagnetic Devices Using FastMag and Distributed Evolutionary Algorithms" *IEEE Transactions on Magnetics, Vol. 52/Issue 9,* May 04, 2016.

Sidi Fu, Weilong Cui, Matthew Hu, Ruinan Chang, Michael J. Donahue, and Vitaliy Lomakin, "Finite-Difference Micromagnetic Solvers With the Objective-Oriented Micromagnetic Framework on Graphics Processing Unit" *IEEE Transactions on Magnetics, Volume 52, April,* 2016.

A. Shlivinski, and V. Lomakin, "Gaussian-Windowed Frame Based Method of Moments Formulation of Surface-Integral-Equation for Extended Aperatures" *Journal of Computational Science, Vol. 308,* March 1, 2016.

#### **Professor Paul H. Siegel**

Veeresh Taranalli, Hironori Uchikawa, and Paul H. Siegel, "On the Capacity of the Beta-Binomial Channel Model for Multi-Level Cell Flash Memories, " to appear in IEEE Journal on Selected Areas in Communications, 2016.

Pengfei Huang, Paul H. Siegel, and EitanYaakobi, "Performance of Flash Memories with Different Binary Labelings: A Multi-User Perspective," to appear in IEEE Journal on Selected Areas in Communications, 2016.

Veeresh Taranalli, Hironori Uchikawa, Paul H. Siegel, "Channel Models for Multi-Level Cell Flash Memories Based on Empirical Error Analysis," IEEE Transactions on Communications, vol. 64, no. 8, August 2016, pp. 3169-3181.

Sarit Buzaglo, Eitan Yaakobi, Yuval Cassuto, and Paul H. Siegel, "Consecutive Switch Codes," IEEE International Symposium on Information Theory (ISIT), Barcelona, Spain, July 2016, pp. 660-664.

#### **Professor Frank Talke**

Y. Fu, V. A. Lubarda, and **F.E. Talke**, "The effect of diamond-like carbon overcoat on the tribological performance of the dimple/gimbal interface in hard disk drives," J. Tribol., Feb. 2016.

Y. Fu, C. Zhang, A. Ovcharenko, M. Yang, and **F.E. Talke**, "Modeling of thermal sensor response to disk asperities," to be published in IEEE Transactions on Magnetics, 2016

Y. Fu, M. Yang, J. P. Peng, and **F. E. Talke**, "Wear between lift tab and load/unload ramp in hard disk drives," to be published in IEEE Transactions on Magnetics, 2016

K. Morris, L. Matthes, F.E. Spada, A. Ovcharenko, B.E. Knigge and F.E. Talke, "Effect of Solider Bias Voltage and Humidity on Wear and Contact Potential" *ASME 2016 Conference on Information Storage Processing Systems*, June 20-21,2016.